Article

# **Pressure-Dependent Ion Rejection in Nanopores**

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**ABSTRACT:** It is generally considered that ion rejection of a desalination membrane is independent of the operation pressure drops ( $\Delta Ps$ ), which is typically not higher than 10 MPa. However, this may not be true for pressures as high as hundreds of megapascals usually used in simulations. Therefore, simulation results of high  $\Delta Ps$  cannot be directly used to predict real-world ion rejections, which is often overlooked. Herein, we investigate the ion rejection of carbon nanotube membranes in a large scale of  $\Delta Ps$  via nonequilibrium molecular dynamics simulations. With effective pressure drops ( $\Delta P_e$ 's) increased from 2.85 to 996 MPa, the ion rejection drops from 100% to nearly zero. Rather than directly investigating the rejection, the relationships of ion and water fluxes with  $\Delta Ps$  are separately investigated. With rising  $\Delta P_{es}$ , the water flux increases linearly, while the ion flux



undergoes a two-stage increase: first, an exponential increase at  $\Delta P_e \leq 53.4$  MPa and then a linear increase. An equation describing the  $\Delta P_e$ -dependent ion rejection is then developed based on these observations. Moreover, the rejection mechanism is also discovered, which indicates that the enhanced input energy makes ions easier to overcome the energy barrier rather than the molecular-configurational reasons. These findings are expected to fill the big gaps between simulations and experiments and may also be helpful for the rational design of the next-generation desalination membranes.

## 1. INTRODUCTION

The growing demand for freshwater is currently one of the major global issues. As an energy-efficient and cost-effective way, reverse osmosis (RO) technology can provide potable water to alleviate the water scarcity and is currently playing a dominating role in the desalination market.<sup>1</sup> However, the commonly used polymeric RO membranes have their own bottlenecks such as a trade-off effect between water permeance and salt rejection.<sup>2</sup> Thus, tremendous efforts were made to maximize the water permeance without sacrificing the salt rejection.<sup>3</sup> Usually, the drive to significantly enhance water permeance requires developments in new materials.<sup>4</sup>

The newly emerged nanomaterials with the angstrom-scale pores are alternatives for fabricating high-performance desalination membranes. Taking graphene oxide (GO) membranes as examples, there exists the ultrafast water transport through the confined channels. The extraordinary water permeation is attributed to the slip flow through the atomically smooth and unoxidized graphene channels.<sup>5</sup> Therefore, many efforts were made to fabricate the lamellar GO membranes for desalination.<sup>6-8</sup> Besides GO, it was found that fast water transport also exists in many other twodimensional (2D) nanomaterials, such as molybdenum disulfide  $(MoS_2)^9$  and hexagonal boron nitride (h-BN).<sup>10</sup> Because the unusual water flow under extreme confinement is beyond the classic continuum hydrodynamics, development in membranes using these nanomaterials as building blocks often needs guidance from molecular-level understandings.11 However, the fluid transport through these membranes is hardly observed directly by existing experimental characterizations.

In the angstrom-scale confinement, nonequilibrium molecular dynamics (NEMD) simulations are practical and powerful techniques to simulate the pressure-driven membrane separation processes. By performing experiments on computers, it is feasible to make comprehensive understandings of transport properties, including both macroscopic behaviors of fluids (e.g., flux) as well as molecular details of transport behaviors. By investigating the effects of pore size and chemical functionalization on desalination performance, Cohen-Tanugi and Grossman revealed that the nanoporous graphene enabled two to three orders of magnitudes higher water permeance than traditional RO membranes.<sup>12</sup> Compared to the nanoporous graphene, the water permeance of the single-layer  $MoS_2$  nanopore was reported to be increased by ~70% thanks to the hourglass geometry of nanopores.<sup>13</sup> Cao et al. reported that the water permeance of the 2D metal-organic framework was one order of magnitude higher than the nanoporous graphene or  $MoS_2$ .<sup>14</sup> Through NEMD simulations, many other membrane materials were reported to possess outstanding desalination performances, for example, GO,<sup>15</sup> graphyne,<sup>16</sup>, and covalent organic framework (COF).<sup>18</sup>

However, the overwhelming majority of NEMD simulations use very high pressure drops ( $\Delta Ps$ ), typically 100–1000 MPa,

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which is two to three orders of magnitude higher than the realistic operating pressures, which are typically 1-10 MPa.<sup>12-14,19,20</sup> Such a high- $\Delta P$  method was first proposed by Zhu et al. in 2002 and used to enhance the signal-to-noise ratio and the computational efficiency in the limited simulation time.<sup>21</sup> The prior computational work reported by Leung and Rempe investigated the effect of varying  $\Delta Ps$  on salt passage.<sup>22</sup> It was pointed out that the ion rejection would significantly decrease with increased  $\Delta Ps$  in nanoporous membranes. Unfortunately, the quantitative relationship between ion rejection and  $\Delta P$  remains elusive. In most cases, the effect of  $\Delta P$  on the ion rejection is overlooked. That is, the ion rejection in the high- $\Delta P$  simulation is directly regarded as that at experimentally low  $\Delta P$ . In some works, the linear relationship between salt rejection and  $\Delta P$  was assumed, <sup>12,16,23</sup> but this assumption is problematic because it does not have a solid theoretical basis. Cohen-Tanugi and Grossman used a rough kinetic model to qualitatively describe the decreased salt rejection with increased  $\Delta Ps$ .<sup>12</sup> Thomas and Corry reported that salt rejection would significantly decrease with enhanced  $\Delta Ps$ , and revealed that the 1.1 nm-wide carbon nanotube (CNT) with poor rejection in the high- $\Delta P$  simulation may afford the experimentally high ion rejection.<sup>24</sup> Therefore, the ion rejection from NEMD simulation results cannot accurately predict the experimental performance because of the vast difference in  $\Delta Ps$ .

Establishing the relationship of ion rejections with  $\Delta Ps$  and understanding the rejection mechanisms are of great significance to accurately assess the ion rejection performance from the NEMD simulation results. In this study, the CNT is chosen as the pore model because its nonpolar, inert, and smooth surface can exclude the possible adsorption of ions on pores, which is beneficial to analyze the mechanisms. The ion rejection performances of CNTs with various  $\Delta Ps$  from 10 to 1000 MPa are investigated via NEMD simulations. Because ion rejection is decided by water and ion fluxes, we develop equations to describe the effective pressure drop ( $\Delta P_e$ )dependent water and ion fluxes, and thus establish the relationship between ion rejection and  $\Delta P_e$ . Such a relationship could extend to the lower  $\Delta Ps$  as the molecular mechanism of ion rejection at low  $\Delta Ps$  is also revealed.

# 2. SIMULATION DETAILS

**2.1. Construction of Models.** The snapshot for the NEMD simulation is shown in Figure 1. In the middle of the system is a CNT, which is enclosed by two graphene sheets with holes matching the CNT diameter. The simulation model also contains a feed chamber on the left and a permeate chamber on the right. Two rigid graphene sheets at the outer ends of the simulation box act as pistons to generate a pressure



**Figure 1.** Modeling of the simulations. Snapshot of the simulated water and ion transport through the CNT membrane. The compositions are labeled in the figure.

drop across the membrane, which pushes saline water across the CNT membrane. The feed chamber contains 58 Na<sup>+</sup> and 58 Cl<sup>-</sup> solvated by 3242 water molecules, corresponding to the salt concentration of 1 mol  $L^{-1}$ . A higher salinity than that of seawater (0.599 mol  $L^{-1}$ ) is used to collect sufficient statistics of ion transport events within the limited simulation time, which is commonly used in simulation works.<sup>13,14,25</sup> The permeate chamber contains 607 water molecules. The x and y dimensions of the simulation system are set to 3.19 and 3.40 nm, respectively. (10, 10) armchair CNT was selected with an effective diameter of 1.01 nm, after deducting the van der Waals diameter of carbon atom (0.34 nm). The effective diameter of 1.01 nm is slightly wider than the one that achieves a complete rejection at 100 MPa,<sup>26</sup> promising the sensitivity of ion rejection to  $\Delta Ps$ . The length of the CNT is set to 2.34 nm, under which the ion rejection may decrease with the length.<sup>26</sup>

2.2. Simulation Protocol. All of the simulations were conducted with the LAMMPS package.<sup>27</sup> All carbon atoms were held rigid. Fixed membranes can prevent the deformation of membranes caused by the pressure, which is widely used in many simulations.<sup>14,25,28</sup> The atom interactions included both the 12-6 Lennard-Jones (LJ) and the Coulombic interactions. The SPC/E water model was used with the SHAKE algorithm that constrains the bonds and angles. Correspondingly, the parameters for Na<sup>+</sup> and Cl<sup>-</sup> were proposed by Joung and Cheatham.<sup>29</sup> The LJ interactions between carbon and oxygen atoms were selected as the parameters:  $\sigma_{\rm C-O} = 0.319$  nm,  $\varepsilon_{\rm C-O}$ =  $0.392 \text{ kJ mol}^{-1.30}$  Lorentz–Berthelot combination rules were employed to generate LJ cross-interaction parameters between different elements. The cutoff distances of LJ potentials and electrostatic interactions were set to 1.0 and 1.2 nm, respectively. Long-range electrostatic interactions were computed by the particle-particle particle-mesh method with the accuracy of  $10^{-4.31}$  Periodic boundary conditions were only applied in x and y dimensions.

For each simulation, energy minimization was first conducted with a tolerance of  $10^{-5}$ . Then, 5 ns equilibrium molecular dynamics simulation was performed at 300 K and 0.1 MPa to allow water molecules to wet CNT membranes. Finally, in the NEMD simulations, the pressure drop ( $\Delta P$ ) across the membrane was generated as

$$\Delta P = P_{\text{feed}} - P_{\text{permeate}} \tag{1}$$

where  $P_{\text{feed}}$  and  $P_{\text{permeate}}$  represent the pressures on the feed and permeate pistons, respectively.  $P_{\text{feed}}$  was set to the desired pressure, and  $P_{\text{permeate}}$  was set to 0.1 MPa (ambient pressure). To generate the desired pressures, the external forces were applied to the atoms of the piston, which can be calculated as

$$f = \frac{PA}{n} \tag{2}$$

where A is the cross-sectional area of the membrane and n is the number of carbon atoms of the piston. The temperature of the system was kept at 300 K with a Nosé–Hoover thermostat. The trajectories were saved every 1 ps with a time step of 1 fs. The  $\Delta P$  ranging from 10 to 1000 MPa was used. Based on the magnitude of the  $\Delta P$ , the simulation time is ranged from 1 to 300 ns so as to allow half number of the water molecules (~1600) in feed chambers to permeate through the membrane at each  $\Delta P$ . To reduce the statistical deviation, the results were calculated by averaging over three separate runs with different sets of initial configurations.



**Figure 2.**  $\Delta P$ -dependent NaCl rejection. (a) NaCl rejection as a function of  $\Delta P$ s ranging from 10 to 1000 MPa. (b) Linear relationship between NaCl rejection and  $\Delta P$  in two short periods of  $\Delta P$ s from 10 to 125 MPa and from 150 to 400 MPa. (c) Osmotic pressure difference ( $\Delta \Pi$ ) as a function of  $\Delta P$ s. (d) NaCl rejection as a function of effective pressure drops ( $\Delta P_e$ 's) from 2.85 to 996 MPa. Insets for (a,c,d) are zoomed in 0–105 MPa.

**2.3.** Post-Simulation Analysis. As shown in Figure S1, the number of water molecules permeated through the CNT membrane increases linearly with the sampling time, which means that the water flow is in a steady state. The water flux was calculated by the slope of the number of water molecules permeated through the membrane with the sampling time (Figure S1). Besides, ion rejection (R) is defined as

$$R = 1 - \frac{c_{\rm p}}{c_{\rm f}} \tag{3}$$

where  $c_p$  and  $c_f$  represent the ion concentrations in the permeate and feed sides, respectively. Herein, R = 100% means that only water molecules can pass through the membrane, while R = 0% means that the ion concentration of the permeate solution is equal to that of the initial feed solution. Based on  $c_p = F_i/F_w$  and  $c_f = n_i/n_w$ , R can be calculated in a detailed expression as below

$$R = 1 - \frac{F_{\rm i}/F_{\rm w}}{n_{\rm i}/n_{\rm w}} \tag{4}$$

where  $F_i$  and  $F_w$  are water and ion fluxes, respectively. The number of ions and water passing through the membrane during a span of simulation time was counted to calculate  $F_i$ and  $F_w$ .  $n_i$  and  $n_w$  are the initial number of ions and water molecules in the feed side, which is equal to 58 and 3242, respectively. Obviously, ion rejection is dependent on  $F_i$  and  $F_w$ . Therefore, in order to establish the relationship between ion rejection and  $\Delta P$ , the relationships of  $F_i$  and  $F_w$  with  $\Delta Ps$ are investigated in the following analysis.

## 3. RESULTS AND DISCUSSION

**3.1. Dependence of lon Rejection on**  $\Delta Ps$ . We first investigate NaCl rejection with  $\Delta P$  ranging from 10 to 1000 MPa. As shown in Figure 2a, the ion rejection is highly dependent on the applied  $\Delta Ps$ . When  $\Delta P$  decreases from 1000

to 400 MPa, the ion rejection maintains ~4%. When  $\Delta P$  decreases from 400 to 10 MPa, the ion rejection will increase gradually from 4 to 100%. To accurately describe the  $\Delta P$ -dependent ion rejections, the intervals of  $\Delta P$ s are smaller when the changes of ion rejections are faster, which are 5, 25, and 100 MPa with  $\Delta P$ s of 10–100, 100–350, and 400–1000 MPa, respectively. Enhanced ion rejections with decreased  $\Delta P$ s were also reported in many other materials, for example, graphene,<sup>12</sup> graphyne,<sup>16</sup> and COFs,<sup>32</sup> the staking layered structure of which afford one-dimensional straight pores such as CNTs.

In NEMD simulations, the  $\Delta P$  of 100 MPa is often used,<sup>12-14</sup> and the corresponding ion rejection is 49%. This result indicates that the 1.01 nm-wide CNT membrane is undesirable for desalination. However, if the  $\Delta P$  is 10 MPa, which is near to the usual experimental or industrial operation condition,<sup>33</sup> the ion rejection is as high as 100%, which is absolutely desirable for desalination. Therefore, the results of high- $\Delta P$  simulations are not reliable to predict the ion rejection performances.

The findings from high- $\Delta P$  simulations will underestimate the experimental ion rejection performance. In other words, a wider nanopore with poor rejection at high  $\Delta P$  may also be desirable for desalination because its ion rejection performance is much better at low  $\Delta P$ . For example, the previously reported maximum diameter for complete salt rejection of CNTs is 0.88 nm at 100 MPa.<sup>26</sup> If the pore diameter increases from 0.88 to 1.01 nm, the NaCl rejections are all 100% at experimental operation conditions. However, the water permeance of the 1.01 nm-wide CNT is dramatically increased from 545.6 to 1270 L m<sup>-2</sup> h<sup>-1</sup> bar<sup>-1</sup> compared to the 0.88 nm-wide CNT. Therefore, the underestimation will of course mislead the design of new membranes.

Because the effect of  $\Delta P$  on the ion rejection is pronounced, it is important to figure out the origin of this observation and to develop an equation to describe the  $\Delta P$ -dependent ion rejection. As it is widely assumed a linear relationship in the



**Figure 3.** Water and ion fluxes with the relationship of  $\Delta P_e$ 's. (a) Water flux as a function of  $\Delta P_e$ 's ranging from 2.85 to 996 MPa. The inset is zoomed in 0–105 MPa. (b) Ion flux as a function of  $\Delta P_e$  ranging from 2.85 to 996 MPa. The linear fitting is only applied to 58.2–996 MPa. The inset is zoomed in 0–210 MPa. (c) PMFs for Cl<sup>-</sup>, Na<sup>+</sup>, and water molecules passing through the CNT membrane. The two gray dashed lines denote the positions of the entrance and exit of the membrane. (d) Ion flux as a function of  $\Delta P_e$  ranging from 2.85 to 53.4 MPa. Equation 9 is used to fit the data.

literature, <sup>12,14,16</sup> we try to use this relationship to fit the data. As shown in Figure 2b, the likely linear relationship is only observed in two short periods of  $\Delta Ps$  of 10–125 and 150–400 MPa. Obviously, the linear relationship cannot fit the data well in the whole range of  $\Delta Ps$ .

It is well-known that the applied  $\Delta P$  is directly affected by the osmotic pressure difference ( $\Delta\Pi$ ).  $\Delta\Pi$  originated from the ionic concentration difference should be deducted from  $\Delta P$ . The previous study using the same force fields of water and ion as our simulations showed that the calculated osmotic pressure is highly consistent with experiments and the van't Hoff equation at NaCl concentrations below 2 mol  $L^{-1,34}$ . Therefore,  $\Delta \Pi$  is calculated by the van't Hoff equation and the calculation details are shown in the Supporting Information. As shown in Figure 2c, with  $\Delta P$  decreased from 1000 to 400 MPa,  $\Delta\Pi$  maintains around 3.57 MPa. When  $\Delta P$ decreases from 400 to 10 MPa,  $\Delta\Pi$  is sharply increased from 3.57 to 8.15 MPa. The effect of  $\Delta \Pi$  on  $\Delta P$  is significant at low  $\Delta Ps$ , but negligible at high  $\Delta Ps$ .  $\Delta \Pi$  is highly dependent on salt rejection because a higher salt rejection will lead to a higher concentrated solution of the feed side in a limited simulation box. It should be noted that the calculated  $\Delta \Pi s$  are much higher than that in experiments for two reasons. First, the initial salt concentration of 1 mol  $L^{-1}$  in the feed side is much higher than that commonly used in experiments  $(\sim 0.0342 \text{ mol } L^{-1})$ .<sup>33</sup> The other reason is that the limited simulation box will increase the concentration difference, especially when the rejection is high. In addition, the abovecalculated  $\Delta \Pi$  is the average value during the filtration process. The instantaneous  $\Delta \Pi$  can reach a maximum of 10 MPa at the concentration difference of 2 mol  $L^{-1}$ , which is equal to the applied minimum  $\Delta P$  of 10 MPa. In this situation, we find that at most half of the water molecules in the feed chamber are permeated through the membrane, which is nearly independent of the sampling time. Therefore, to accurately calculate the water and ion fluxes, we collect the data during 40% of water molecules in the feed chamber permeated through the membrane at the  $\Delta P$  of 10 MPa.

To exclude the effect of  $\Delta \Pi$  on  $\Delta P$ , the effective pressure drop  $(\Delta P_{\rm e})$  is defined as

$$\Delta P_{\rm e} = \Delta P - \Delta \Pi \tag{5}$$

In order to overcome  $\Delta\Pi s$ , the  $\Delta Ps$  used in this work are higher than 10 MPa. Therefore, the minimum of the effective pressure drop ( $\Delta P_e$ ) is in the range of the experimental operations. As  $\Delta P$  increases from 10 to 1000 MPa,  $\Delta P_e$  is increased from 2.85 to 996 MPa. As shown in Figure 2d, the relationship between ion rejection and  $\Delta P_e$  is nearly unchanged compared to  $\Delta P$ . It is also difficult to find a direct relationship between ion rejection and  $\Delta P_e$ . From eq 4, it is obvious that ion rejection is decided by the water flux ( $F_w$ ) and the ion flux ( $F_i$ ). We then investigate  $F_w$  and  $F_i$  with the relationship of  $\Delta P_e$ 's.

**3.2. Dependence of Water and Ion Fluxes on \Delta Ps.** Water flux as a function of  $\Delta P_e$ 's is shown in Figure 3a. As expected from the continuum hydrodynamics, there is a finely linear and zero-axial relationship between water flux and  $\Delta P_e$  as shown below

$$F_{\rm w} = 1.344 \Delta P_{\rm e} \tag{6}$$

Although the classical continuum hydrodynamics is not sufficiently reasonable to explain the behaviors of water under extreme confinement,<sup>35</sup> this empirical linear relationship was previously reported.<sup>36–38</sup> Based on this linear relationship, the high- $\Delta P_{\rm e}$  water flux can be extrapolated to the low- $\Delta P_{\rm e}$  water flux.

After establishing the relationship between  $F_{w}$  and  $\Delta P_{e}$ , we then try to figure out the relationship between  $F_{i}$  and  $\Delta P_{e}$ . As



Figure 4. Relationship between ion rejection and  $\Delta P_e$ : (a)  $\Delta P_e$  from 2.85 to 53.4 MPa; (b)  $\Delta P_e$  from 58.2 to 996 MPa. The blue symbols are the simulation data, and the red curves are plotted by eq 11.

shown in Figure 3b,  $F_i$  shows a monotonic increase with  $\Delta P_e$  increased from 2.85 to 996 MPa. Similar to  $F_w$ , there seems a linear increase in  $F_i$  with  $\Delta P_e$ . The linear relationship is sufficiently reasonable to describe  $F_i$  with  $\Delta P_e$  from 58.2 to 996 MPa. It is found that the magnitude of  $F_i$  is much less than that of  $F_w$  because the ion concentration is much lower than the water concentration.

However, as shown in the inset of Figure 3b, when  $\Delta P_e$  is <58.2 MPa,  $F_i$  decreases slower and drifts away from the linearly fitted line. In this period of  $\Delta P_{e^*}$  there should be another relationship. Based on the Arrhenius model, eq 7 is often assumed to describe  $F_i$  as it is in direct proportion to the reaction rate constant.<sup>12,39,40</sup>

$$F_{\rm i} \propto {\rm e}^{-\Delta G/kT} \tag{7}$$

where  $\Delta G$  is the free energy barrier for ion passing through the membrane, k is the Boltzmann's constant of  $1.381 \times 10^{-23}$  J  $K^{-1}$ , and T is the liquid temperature of 300 K. From eq 7,  $F_i$  is only dependent on  $\Delta G$ , and a higher  $\Delta G$  will lead to a smaller  $F_{i}$ , and vice versa. The magnitude of  $\Delta G$  is obtained from the potential of mean force (PMF). The calculation details of PMF are shown in the Supporting Information. As shown in Figure 3c, the  $\Delta G$  for Cl<sup>-</sup> of 4.72 kcal mol<sup>-1</sup> is higher than that for Na<sup>+</sup> of 4.09 kcal mol<sup>-1</sup>. This observation is because a larger hydration shell of Cl<sup>-</sup> has to peel off more water molecules while entering nanopores compared to Na<sup>+</sup>. Because of the higher energy barrier for Cl<sup>-</sup>, Cl<sup>-</sup> is easier to be retained than Na<sup>+</sup>. Once Cl<sup>-</sup> is rejected, the oppositely charged ion of Na<sup>+</sup> will be simultaneously rejected to maintain the charge balance. Therefore, NaCl rejection is decided by Cl<sup>-</sup> rejection. In the following discussions, we will further investigate the relationship between  $F_i$  and  $\Delta P_e$  based on the data of Cl<sup>-</sup>.

Besides  $\Delta G$ , the input energy  $(E_i)$  will also influence ion transport, which can be calculated as

$$E_{\rm i} = V_{\rm i} \Delta P_{\rm e} \tag{8}$$

where  $V_i$  is the effective volume of the hydrated ion. From the radial distribution functions (RDFs) of ions with oxygen atoms of water in Figure S3, the peaks and valleys indicate the formation of the hydration shells, and the hydrated ion can be regarded as a sphere. The radii of the hydrated Cl<sup>-</sup> is 3.775 Å, and thus  $V_i$  is calculated as 225.3 Å<sup>3</sup>. Obviously,  $E_i$  increases linearly with rising  $\Delta P_{e'}$  while  $\Delta G$  is a constant value. Driven by the increased  $E_i$ ,  $F_i$  will increase with rising  $\Delta P_e$  (Figure 3b). Taking both  $\Delta G$  and  $E_i$  into consideration, we can transform eq 7 into a detailed expression as below

$$F_{\rm i} = A_0 \, \mathrm{e}^{(V_{\rm i} \Delta P_{\rm e} - \Delta G)/kT} + F_0 \tag{9}$$

where  $F_0$  and  $A_0$  are set to the fitted parameters. The exponential decrease of  $F_i$  with  $\Delta P_e$  decreased from 53.4 to 2.85 MPa is finely fitted in Figure 3d by using eq 9, and  $F_0$  and  $A_0$  are calculated as -0.04182 and 74.38.

In general, as shown in eq 10,  $F_i$  undergoes first an exponential increase with  $\Delta P_e$  increased from 2.85 to 53.4 MPa and then a linear increase with  $\Delta P_e$  further increased to 996 MPa.

$$F_{\rm i} = \begin{cases} 74.38 \ e^{0.05440\Delta P_{\rm e} - 7.914} - 0.04182 & \Delta P_{\rm e} \le 53.4 \\ 0.02466\Delta P_{\rm e} - 1.212 & \Delta P_{\rm e} > 53.4 \end{cases}$$
(10)

From eq 10, there is a threshold  $\Delta P_e$  where  $F_i$  transforms from an exponential increase to a linear increase. The threshold  $\Delta P_e$  may be determined by both  $\Delta G$  and  $E_i$ . When  $\Delta P_e$  is smaller than 53.4 MPa, the calculated  $E_i$  is smaller than 1.73 kcal mol<sup>-1</sup> based on eq 8, which is much smaller than the  $\Delta G$  of 4.72 kcal mol<sup>-1</sup>. In this situation,  $\Delta G$ plays a dominating role, and thus the modified Arrhenius model as eq 9 can describe the relationship between  $F_i$  and  $\Delta P_e$ . With further increased  $E_v$  it shows a linear relationship between  $F_i$  and  $\Delta P_e$ .

**3.3. Description of \Delta P-Dependent lon Rejections.** By introducing eqs 6 and 10 that describe  $\Delta P_e$ -dependent  $F_i$  and  $F_w$  into eq 4, the relationship between ion rejection and  $\Delta P_e$  can be described as

$$R = \begin{cases} 1 + \frac{1.739 - 3093 e^{0.05440\Delta P_{\rm e} - 7.914}}{\Delta P_{\rm e}} & \Delta P_{\rm e} \le 53.4 \\ \frac{50.41}{\Delta P_{\rm e}} - 0.026 & \Delta P_{\rm e} > 53.4 \end{cases}$$
(11)

The curves of describing  $\Delta P_{e}$ -dependent ion rejection based on eq 11 and the simulation data are shown in Figure 4a,b. When  $\Delta P_{\rm e}$  is smaller than 53.4 MPa, the relationship between ion rejection and  $\Delta P_{\rm e}$  is complicated. Because eq 11 is based on the fittings of ion and water fluxes, it neglects the boundary condition, that is, the ion rejection will slightly exceed 100% (the upper limit of rejection) at  $\Delta P_{\rm e} \leq \sim 7$  MPa. When  $\Delta P_{\rm e}$  is larger than 53.4 MPa, the inversely proportional relationship is sufficiently reasonable to describe the ion rejection. With increased  $\Delta P_{e}$ 's, the ion rejection shows a monotonic decrease and the decreasing rate slows down. When  $\Delta P_{\rm e}$  is larger than 396 MPa ( $\Delta P = 400$  MPa), ion rejection is slightly decreased with rising  $\Delta P_{\rm e}$  based on eq 11, which is consistent with the nearly unchanged ion rejection from simulation results. The applied  $\Delta P$  is typically considered to be no larger than 1000 MPa because water will exist as ice beyond this value based on



Figure 5. Behaviors of ion transport in nanopores. (a) Schematic illustrations of the hydrated  $Cl^-$  with two hydration shells in bulk aqueous solutions (left) and the partially dehydrated  $Cl^-$  at the entrance of CNTs (right). When the partially dehydrated  $Cl^-$  is ready to enter the nanopore, the energy barrier pulls it to return to the bulk aqueous solution, while the input energy pushes it into the nanopore at the same time. Atomic colors: carbon, cyan;  $Cl^-$ , green. The light yellow and grey shadings denote the first and second hydration shells of ions, respectively. The two grey dashed lines represent the entrance and exit of the CNT. (b) Profiles of the average number of water molecules  $(n_w)$  inside the first and second hydration shells of  $Cl^-$  and Na<sup>+</sup> along the *z* direction at 100 MPa. The light organic and blue shadings denote the first and second hydration shells, respectively. (c) Dehydration degree  $(\eta_d)$  of  $Cl^-$  and Na<sup>+</sup> as a function of  $\Delta Ps$ .

the experimental phase diagram.<sup>41</sup> In general, the ion rejection shows a piecewise function of  $\Delta P_e$ 's, which replicates the observed behaviors well. Only when  $\Delta P_e$  is smaller than 53.4 MPa, it can be extrapolated from high to low  $\Delta P_e$ . Otherwise, the ion rejection at very high  $\Delta P_e$  cannot be extrapolated to the realistic low  $\Delta P_e$ . Besides, by introducing eq 11 into eq 5, the relationship between ion rejection and  $\Delta P$  can be established after taking  $\Delta \Pi$  into consideration.

**3.4.** Molecular Mechanisms of  $\Delta P$ -Dependent lon **Rejections.** After developing an equation to describe the  $\Delta P$ -dependent ion rejections, it is also important to figure out the mechanisms from molecular observations. There have been four rejection mechanisms in nanopore separation, which includes (1) molecular sieve; (2) electrostatic repulsion; (3) dehydration barrier; (4) in-pore transport difference.<sup>42,43</sup> As illustrated in our previous studies, the mechanisms of both molecular sieve and electrostatic repulsion can be excluded in inert and neutral CNT pores.<sup>26</sup> The in-pore transport difference is also negligible in nonpolar nanopores such as CNTs.<sup>43</sup> Therefore, the dehydration barrier may play an important role in ion rejections.<sup>42,44-46</sup>

The hydration size of ions can be obtained as the minimums of the RDF curves in Figure S3. The second hydration diameters of Cl<sup>-</sup> and Na<sup>+</sup> are calculated as 1.21 and 1.09 nm, respectively, both of which are larger than the 1.01 nm of the CNT diameter. Therefore, the hydrated ions have to peel off some hydrating water molecules while entering CNT pores (Figure 5a). To observe the process of ion dehydration, the profiles of the average number of water molecules ( $n_w$ ) inside the first and second hydration shell of Cl<sup>-</sup> and Na<sup>+</sup> at 100 MPa are shown in Figure 5b.  $n_w$  in the first hydration shell of ions is constant because the first hydration diameters of ions (Na<sup>+</sup>: 0.64 nm, Cl<sup>-</sup>: 0.76 nm) are smaller than the CNT diameter. However,  $n_w$  in the second hydration shell is sharply decreased when an ion enters the nanopore and recovers when an ion leaves the nanopore. The dehydration of the second hydration shells is the origin of the energy barrier for ions. Besides, the hydrated Cl<sup>-</sup> loses more hydrating water molecules than the Na<sup>+</sup> does, which results in a higher energy barrier for Cl<sup>-</sup> (Figure 3c). Moreover, it should be noted that the ion rejection is determined by not only the pore size but also the membrane hydrophilicity. A hydrophilic membrane with a pore diameter of ~0.8 nm often has moderate rejections to ions because the atoms of the pore wall (oxygen, nitrogen, hydrogen, or some other atoms) will compensate for the hydration loss of ions, which lowers the energy barrier for ion passage.<sup>43</sup> In this study, the hydrophobic CNT pore with a diameter of 1.01 nm has very high rejections at low  $\Delta Ps$  because only the dehydration barrier takes effect on the ion rejection, which is consistent with the reported literature.<sup>24</sup>

We then investigate the effect of  $\Delta P$  on ion dehydration. Herein, the dehydration degree  $(\eta_d)$  of ions is defined as

$$\eta_{\rm d} = 1 - \frac{n_{\rm p}}{n_{\rm b}} \tag{12}$$

where  $n_p$  and  $n_b$  are the average number of water molecules inside the hydration shells of ions in the middle of nanopores (z = 0.6-1.4 nm) and in the bulk aqueous solutions. Figure 5c shows  $\eta_d$  of the first and second hydration shells of ions as a function of  $\Delta Ps$ . It is found that  $\eta_d$  of both first and second hydration shell of ions is nearly unchanged with  $\Delta Ps$ , indicating that the dehydration process is nearly independent of  $\Delta Ps$ . The oscillation of  $\eta_d$  in the second hydration shell is because a higher rejection at a lower  $\Delta P$  will result in fewer ions entering nanopores. With a complete rejection, no ion enters the nanopore, and thus the dehydration process cannot be observed. After all, as  $\Delta P$  does not change the membrane properties and thermodynamic state of ion dehydration, the dehydration mechanism cannot explain the  $\Delta P$ -dependent ion rejections either.

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We then focus on the energy analysis rather than the molecular structure. Ion dehydration is commonly regarded as the origin of the energy barrier for ion transport through inert nanopores.<sup>46</sup> Similar to ion dehydration, water molecules have to rearrange hydrogen bonds to enter CNTs,<sup>37,47</sup> which is the origin of the energy barrier for water transport. As shown in Figure 3c, the energy barrier for water molecules is much lower than that for ions. Therefore, the high rejections are observed at relatively low  $\Delta Ps$ . Besides the effect of the energy barrier, the movement of the partially dehydrated Cl<sup>-</sup> is also decided by the input energy (Figure 5a). With increased  $\Delta P_e$ 's, the higher input energy makes ions easier to overcome the energy barrier, which consequently decreases ion rejections. When the input energy is very large compared to the difference in the energy barrier between ions and water molecules, ions can pass through nanopores easily, and the ion rejection is nearly zero.

It should be noted that the molecular structure of ion transport does not change with the declining  $\Delta P_{\rm e}$ . Hence, eq 9 will work at a lower  $\Delta P_{\rm e}$  of experimental operations. We believe that eq 11 will be valid for predicting the ion rejection performance at the experimental operating conditions.

#### 4. CONCLUSIONS

In summary, we investigate the effect of pressure drop ( $\Delta P$ ) on ion rejection via NEMD simulations. In the 1.01 nm-wide and 2.34 nm-long CNT membrane, it is found that the ion rejection is decreased from 100 to ~4% with  $\Delta P$  increased from 10 to 1000 MPa. Because ion rejection performance is dependent on ion and water fluxes, the effects of  $\Delta P$  on ion and water fluxes are separately investigated. The effective pressure drops ( $\Delta P_e$ 's) rather than  $\Delta P$ s are used to exclude the effect of the osmotic pressure differences.  $\Delta P_{\rm e}$  ranges from 2.85 to 996 MPa, which covers the experimental observations. It is found that the water flux is increased linearly with  $\Delta P_{e}$ , whereas the ion flux undergoes first an exponential increase at  $\Delta P_{\rm e} \leq 53.4$  MPa and then a linear increase if  $\Delta P_{\rm e}$  further increases to 996 MPa. Considering both the water and ion fluxes, we propose an equation to describe the  $\Delta P_e$ -dependent ion rejection. Moreover, the rejection mechanism is revealed. The ion rejection drops with rising  $\Delta P_e$ 's because the enhanced input energy makes ions easier to overcome the energy barrier. These findings warn us to consider the effect of  $\Delta P$  on the ion rejection while using very high  $\Delta Ps$  in simulations. With our proposed equations and the revealed rejection mechanisms, it will be helpful to make a reliable prediction of the experimental ion rejection performance.

## ASSOCIATED CONTENT

#### **Supporting Information**

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jpcc.0c03641.

Illustration of steady-state flows; calculation details of osmotic pressure differences ( $\Delta\Pi s$ ); calculation details of PMFs; RDFs; and simulation results for the enlarged simulation box (PDF)

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#### Notes

The authors declare no competing financial interest.

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